

Ratio-Of-Uniforms Methode

AKVFM Numerische Methoden der Finanz- und Versicherungsmathematik

SS 2006, Reinhold Kainhofer, FAM, TU Wien

Ratio of uniforms, allgemeine Definition

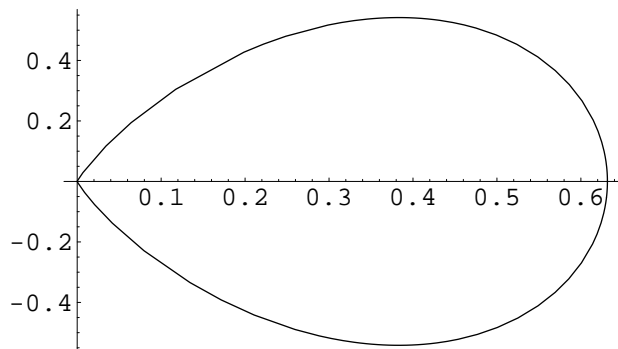
`In[4]:= << Graphics``

Definition des Bereichs A:

```
In[6]:= matches[{x_, y_}, f_] :=  $\left( 0.0001 < x \ \&\& \ x \leq \sqrt{f\left[\frac{y}{x}\right]} \right);$   
bnd[x_, f_] :=  $\{\sqrt{f[x]}, x \sqrt{f[x]}\}$ 
```

ROU fuer Normalverteilung

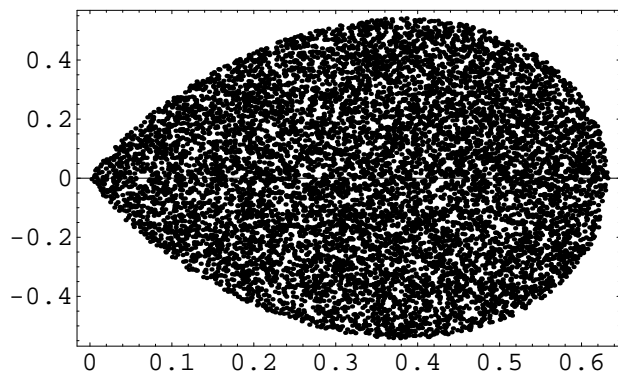
```
In[97]:= fNV01[x_] :=  $\frac{1}{\sqrt{2\pi}} \text{Exp}\left[\frac{-x^2}{2}\right]$ 
ParametricPlot[bnd[x, fNV01], {x, -10, 10}];
```



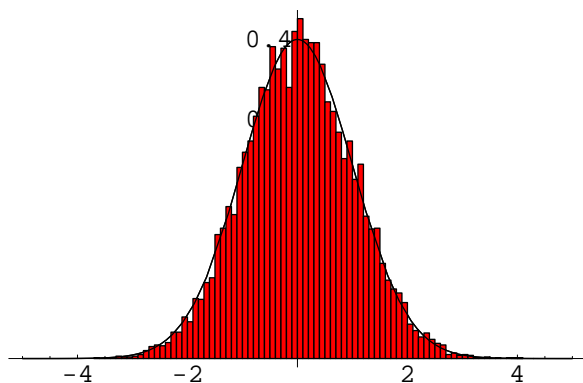
Mit 10000 Zufallszahlen:

```
selectedMC = {}; normalNrsMC = {};
While[Length[selectedMC] < 10000,
  {u, v} = {0.7 Random[], 1.2 Random[] - 0.6};
  If[matches[{u, v}, fNV01],
    AppendTo[selectedMC, {u, v}]; AppendTo[normalNrsMC, v/u];
  ]
```

```
In[83]:= ListPlot[selectedMC, Frame -> True];
```



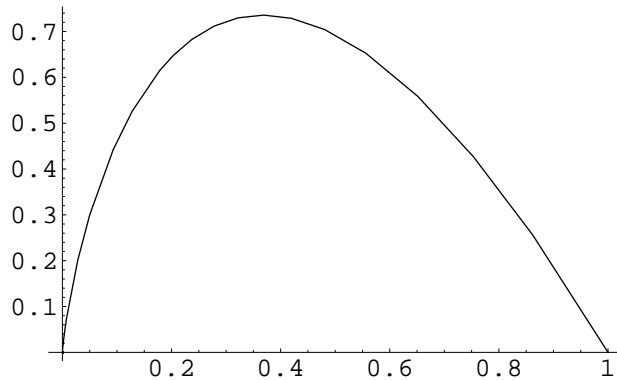
```
In[87]:= hist = Histogram[normalNrsMC, HistogramScale -> 1, DisplayFunction -> Identity];
densplot = Plot[fNV01[x], {x, -5, 5}, DisplayFunction -> Identity];
Show[{densplot, hist, densplot}, DisplayFunction -> $DisplayFunction];
```



ROU fuer Exponentialverteilung

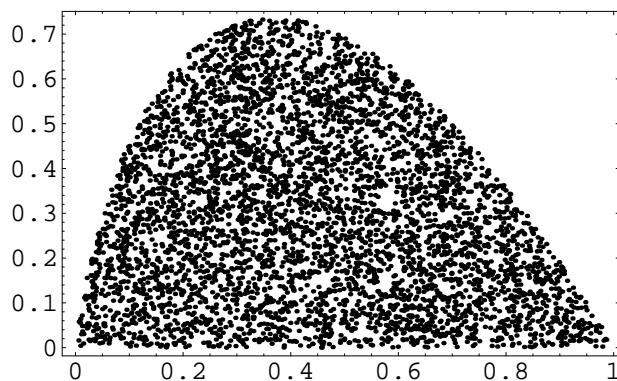
```
In[29]:= fExp[x_] := Exp[-x]
```

```
In[60]:= ParametricPlot[bnd[x, fExp], {x, 0, 5000}, PlotPoints -> 500];
```

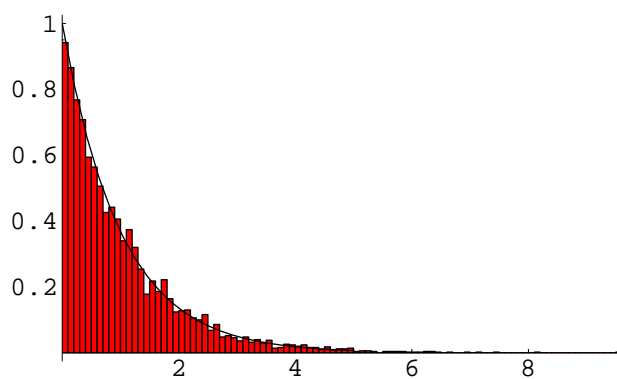


```
selectedMC = {}; nrsMC = {};
While[Length[selectedMC] < 5000,
  {u, v} = {Random[], (2/E) Random[]};
  If[matches[{u, v}, fExp], AppendTo[selectedMC, {u, v}]; AppendTo[nrsMC, v/u];
]
```

```
In[67]:= ListPlot[selectedMC, Frame -> True];
```



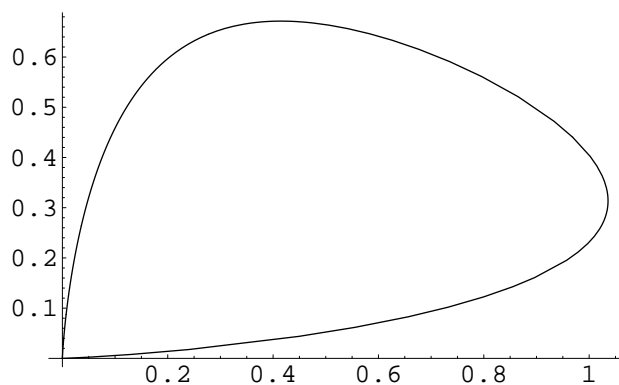
```
In[68]:= hist = Histogram[nrsMC, HistogramScale -> 1,
  PlotRange -> {{0, 5}, {0, 1}}, DisplayFunction -> Identity];
densplot = Plot[fExp[x], {x, 0, 5}, DisplayFunction -> Identity];
Show[{hist, densplot}, DisplayFunction -> $DisplayFunction];
```



ROU fuer IG

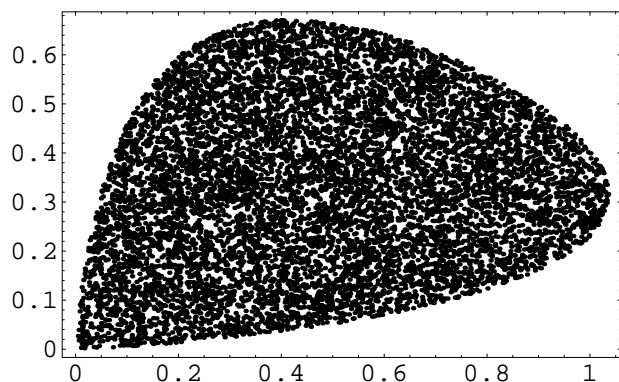
```
In[51]:= FIG[x_] :=  $\delta \frac{\text{Exp}[\delta \gamma]}{\sqrt{2 \pi}} x^{-3/2} \text{Exp}\left[\frac{-1}{2} \left(\delta^2 \frac{1}{x} + \gamma^2 x\right)\right];$ 
```

```
In[96]:= ParametricPlot[bnd[x, FIG], {x, 0, 50}, PlotPoints → 500, PlotRange → All];
```



```
 $\delta = 1; \gamma = 1;$ 
selectedMC = {}; nrsMC = {};
While[Length[selectedMC] < 10000,
  {u, v} = {1.2 Random[], 0.8 (Random[])};
  If[matches[{u, v}, FIG], AppendTo[selectedMC, {u, v}]; AppendTo[nrsMC, v/u];
]
```

```
In[56]:= ListPlot[selectedMC, Frame → True];
```



```
In[57]:= hist = Histogram[nrsMC, HistogramScale → 1,
  PlotRange → {{0, 5}, {0, 1}}, DisplayFunction → Identity];
densplot = Plot[FIG[x], {x, 0, 5}, DisplayFunction → Identity];
Show[{hist, densplot}, DisplayFunction → $DisplayFunction];
```

